OFDM Channel Estimation Along with Denoising Approach under Small SNR Environment using SSA

E. Hari Krishna, K. Sivani and K. Ashoka Reddy

Abstract—In this paper, a de-noising approach in conjunction with channel estimation (CE) algorithm for OFDM systems using singular spectrum analysis (SSA) is presented. In the proposed algorithm, the initial CE is computed with the aid of traditional linear minimum mean square error (LMMSE) algorithm, and then further channel is evaluated by considering the low rank eigenvalue approximation of channel correlation matrix related to channel using SSA. Simulation results on bit error rate (BER) revealed that the method attains an improvement of 7 dB, 5 dB and 3 dB compared to common LSE, MMSE and SVD based methods respectively. With the help of statistical correlation coefficient (C) and kurtosis (k), the SSA method utilized to de-noise the received OFDM signal in addition to CE. In the process of denoising, the received OFDM signal will be decomposed into different empirical orthogonal functions (EOFs) based on the singular values. It was established that the correlation coefficients worked well in identifying useful EOFs only up to moderate SNR≥ 12dB. For low SNR<12 dB, kurtosis was found to be a useful measure for identifying the useful EOFs. In addition to outperforming the existing methods, with this de-noising approach, the mean square error (MSE) of channel estimator is further improved approximately 1 dB more in SNR at the cost of computational complexity.

Index Terms—BER, Channel Estimation, OFDM, SVD, SSA, Wireless Communications.

I. Introduction

Orthogonal frequency division multiplexing (OFDM) has been accepted globally to cater the need of data rate requirement of multimedia communication systems. With advances in signal processing algorithms the multiple-input multiple-output (MIMO) with OFDM is considered as the vital

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methods [1]-[3]. Channel estimation (CE) plays a key role in these systems. In [1], the channel correlation matrix is made low rank by singular value decomposition (SVD) was presented to reduce the complexity of channel matrix inversion. Interpolation methods with pilot-based methodologies i.e. like block-type and comb-type arrangements are widely used for OFDM CE to better identify the channel properties [2]-[5]. These methods result in reduced efficiency because of transmission of training data additionally to the original data. Mathematical signal processing operations such as least squares (LS) and minimum mean square error (MMSE) estimators were deployed for OFDM CE [7]-[8]; majority of CE methods are the modified forms of LS estimation (LSE) and MMSE. To reduce the computational complexity, both time and frequency interpolation is employed for massive MIMO-OFDM systems based on DFT with utilizing different pilot patterns is presented [9]. The Krylov subspace technique with multi-stage nested Wiener filter (MSNWF) for low rank approximation is presented in [10] for OFDM CE. All forms of OFDM CE methods and its challenges were best illustrated in [11]-[12]. A different strategy of pilot patterns along with basic OFDM blocks was presented in [13] for OFDM CE under multipath fading channels, it jointly estimates the channel and carrier frequency offset (CFO) in a semi blind approach.

Without use of channel statistics and pilot tones, a coded neural network based method was presented in [14]. To further improve the accuracy of OFDM CE, lower modulation schemes with blind CE [15], and low rank approximation for OFDM CE [16] were presented. In similar lines, a novel blind subspace approach was presented in [17] by combining minor component analysis (MCA) and independent component analysis (ICA). LMMSE estimation using artificial channel attempts made in [18], which eliminates the channel covariance matrix. De-noising approaches based OFDM CE was presented in [19]-[20], which inspired us to use singular spectrum analysis (SSA) technique in conjunction with statistical analysis for CE and de-noising. In order to reduce the complexity of algorithms, learning automata based channel estimation was presented in [21]. MIMO-OFDM channel estimation using compressive sensing based LSE and MMSE was described in [22] and the nonlinear mode decomposition

method and its application to wireless communication was presented in [23].

In [24] the de-noising of received OFDM symbol with decomposed highly correlated empirical orthogonal functions (EOFs) using statistical correlation analysis, worked well for high signal to noise ratios (SNR). But under small SNR, the performance is degraded. In order to improve the performance even under small SNR scenario, we proposed the use of statistical kurtosis analysis in addition to correlation, which was presented in the next sections. Section II describes the mathematical background of basic wireless OFDM transceiver system, section III presents the proposed signal processing method based on SSA and its use in channel estimation (CE) along with de-noising. Finally, section III depicts simulation results and conclusions in section IV.

II. WIRELESS OFDM TRANSCEIVER SYSTEM

The typical wireless OFDM transmitter, as depicted in fig.1, modifies the input binary data b_T onto PSK/QAM mapper $F_b(k)$ and then implements IFFT on parallel transformed data.

$$f_b(n) = \sum_{k=0}^{N-1} F_b(k) e^{j2\pi nk/N}, n = 0, 1, 2, \dots, N-1$$
 (1)

where N is the number of sub carriers. For data $f_b(n)$, the cyclic prefix (CP) is added to ensure zero ISI, $f_{cp}(n)$ is then changed to a domain suitable for wireless OFDM broadcasting.

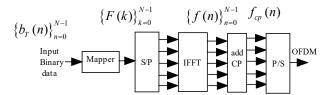


Fig. 1. Typical OFDM transmitter model

Figure 2 shows the receiver model showing proposed channel estimation and de-noising blocks using SSA. The digital converted signal at OFDM receiver can be viewed as

$$y_R(n) = f_{CP}(n) \otimes h_{CIR}(n,k) + w(n)$$
 (2)

where \otimes symbol indicates the convolution; w(n) and $h_{CIR}(n)$ are additive white Gaussian noise (AWGN) with zero mean and unit variance and the channel impulse response (CIR) to be estimated respectively. In general, the channel is non-linear time varying wireless multipath fading channel and the $h_{CIR}(n)$ can be modeled as

$$h(t,\tau) = \sum_{M=0}^{N-1} \tilde{\alpha}_M(t) e^{j\omega_M(t)} \delta(t - \tau_M(t))$$
 (3)

where, k_i , $\alpha_i(n)$ and w(n) are delay incurred, corresponding attenuation and unit sample response occurred in i^{th} path. $\omega_M(t)$ represents the angular Doppler frequency shift due to

time varying. Finally, the received OFDM signal $y_R(n)$ is represented in frequency domain as i.e. Fourier transform of eq (2)

$$Y_{R}(k) = F_{cn}(k)H_{CIR}(k) + W(k)$$
(4)

The $Y_R(k)$ is now used for channel estimation. The time varying CIR is to be properly estimated to perfectly recover the original transmitted binary sequence.

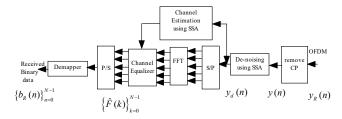


Fig. 2. OFDM Receiver model showing propsed channel estimation and denoising blocks using SSA

Broom-head and King [25]-[26] developed the methodological steps for SSA as shown in Fig. 3:

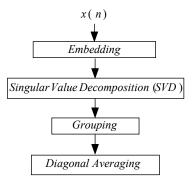


Fig. 3. SSA processing steps

As depicted in Fig. 3, the embedding and SVD are part of decomposition; grouping and diagonal averaging comes under reconstruction stage.

A. Decomposition

i. Embedding

The first step in the decomposition step of basic SSA algorithm is the embedding, where the data is changed into the trajectory matrix consists of overlapped data segments. Let the data be $x = \{x_1 \dots x_n\}$. In the embedding step, window length L is considered in such a way that, where 2 < L < N/2 to embed the initial data. T_X is written as

$$T_{i,j} = \begin{pmatrix} x_1 & x_2 \dots & x_L \\ x_2 & x_3 & \ddots & x_{L+1} \\ \dots & \dots & \dots \\ x_k \dots & \dots & x_N \end{pmatrix}$$
 (5)

ii. Singular value decomposition (SVD)

After the embedding step, apply SVD to the trajectory matrix T_X and obtain the decomposed trajectory matrices T_i for

i=1,...L. The outcome of applying SVD to T_X decomposes as $T_X = UVD'$ called as eigentriples. U_i for 1 < i < L is a $K \times L$ orthogonal matrix. D_i for 1 < i < L is a diagonal matrix order of L. V_i for 1 < i < L is $L \times L$ square orthonormal matrix. In this step T_X , has L many singular values which are $\sqrt{\lambda_1} > \sqrt{\lambda_2}$ $> \sqrt{\lambda_L} >$ thus the i^{th} eigentriple of T_i can be written as $U_i \times \sqrt{\lambda_i} \times V_i^T$ for i=1,2,...,d, So the trajectory matrix T_X can be denoted as

$$T_{x} = T_{1} + T_{2} + \dots + T_{d}$$

$$= U_{1} \sqrt{\lambda_{1}} V_{1}^{T} + \dots + U_{d} \sqrt{\lambda_{d}} V_{d}^{T}$$

$$= \sum_{i=1}^{d} U_{i} \sqrt{\lambda_{i}} V_{i}^{T}$$

$$(6)$$

B. Reconstruction

i. Regrouping

The grouping step of the reconstruction stage is decomposing the $L \times K$ matrix T_i into subgroups. The grouping step of the reconstruction stage is a partition of the set of indices $\{1,2,...d\}$ into the collection of m disjoint subsets of $I = \{I_1,...,I_m\}$. T_{I_i} is a sum of T_j , where $j \in I_i$ so T_x can be expanded as

$$T_{x} = \overbrace{T_{1} + \dots + T_{L}}^{SVD}$$

$$= \overbrace{T_{I_{i}} + \dots + T_{I_{m}}}^{Grouping}$$
(7)

ii. Diagonal Averaging

In this step is to transform the grouping matrices T_{I_i} into a new time series of length N.

$$T_{i,j} = \begin{cases} \frac{1}{s-1} \sum_{j=1}^{s-1} x_{j,s-j} & \text{for } 2 \le s \le L \\ \frac{1}{L} \sum_{j=1}^{L} x_{j,s-j} & \text{for } L+1 \le s \le K+1 \\ \frac{1}{N-s+2} \sum_{i=s-K}^{N-s+2} x_{j,s-j} & \text{for } K+2 \le s \le N+1 \end{cases}$$
(8)

III. PROPOSED SIGNAL PROCESSING METHOD BASED ON SSA

In this proposed method, similar lines as done in SVD, using the traditional LMMSE method the initial CE will be done; and then the channel will be tracked by performing the rank reduction of channel correlation matrix for optimum complexity using SSA. Previously in [1], the approximation is done using SVD, but it was assumed that the channel was slow fading i.e. the channel is unaltered during broadcast of one OFDM signal. Here, that assumption is eliminated in this proposed method.

A. LMMSE Estimation

Let $b_T(n)$ = the transmitted symbol, $y_R(n)$ = the received symbols, h_{CIR} = the assumed CIR, \hat{h}_{CIR} = the estimated CIR

using proposed SSA based method based and \hat{h}_{CIRL} = the estimated CIR using the least squares (LS) estimated channel,

$$Y = [y_R(0), y_R(1), \dots, y_R(N-1)]^T$$
 (5)

$$B = [b_T(0), b_T(1), \dots b_T(N-1)]^T$$
 (6)

$$h_{CIR} = [h_{CIR}(0), h_{CIR}(1), \dots h_{CIR}(N-1)]^{T}$$
(7)

$$\hat{h}_{CIR} = \left[\hat{h}_{CIR}(0), \hat{h}_{CIR}(1), \dots, \hat{h}_{CIR}(N-1) \right]^{T}$$
 (8)

$$\hat{h}_{CIRL} = \left[\hat{h}_{CIRL}(0), \hat{h}_{CIRL}(1), \dots, \hat{h}_{CIRL}(N-1) \right]^{T}$$
(9)

The LMMSE estimated CIR is [1]

$$\hat{H}_{CIRLE} = R_{H_{CIR}\hat{H}_{CIRL}} R_{\hat{H}_{CIRL}\hat{H}_{CIRL}}^{-1} \hat{H}_{CIRL}$$

$$\tag{10}$$

The vector notation of above defined variables is given below

$$=R_{H_{CIR}H_{CIR}}\left(R_{H_{CIR}H_{CIR}}+\sigma_n^2\left(BB^H\right)^{-1}\right)^{-1}\hat{H}_{CIRL}$$

 \hat{H}_{CIRI} is transform domain LS estimated CIR

$$R_{H_{CIR}H_{CIR}} = E\left\{H_{CIR}H_{CIR}^{H}\right\} \tag{11}$$

$$R_{H_{CIR}\hat{H}_{CIRL}} = E\left\{H_{CIR}\,\hat{H}_{CIRL}^{H}\right\} \tag{12}$$

$$R_{\hat{H}_{CIRL}\hat{H}_{CIRL}} = E\left\{\hat{H}_{CIRL}\,\hat{H}_{CIRL}^{H}\right\} \tag{13}$$

To reduce the complexity, the matrix inversion in equation (10), is replaced with average of communicated data [1]. Initially, CE is computed with the aid of traditional LMMSE, and then further channel is evaluated using matrix related to channel

$$\hat{H}_{CIR} = R_{H_{CIR}H_{CIR}} \left(R_{H_{CIR}H_{CIR}} + \frac{\beta}{SNR} I \right)^{-1} \hat{H}_{CIRL}$$
 (14)

Finally, the estimated CIR is uniquely proportional to correlation matrix, so the same $R_{H_{CIR}H_{CIR}}$ is now reduced to low rank using SVD method [1]. In the SVD method, it was assumed as that the channel was slow fading i.e. the channel is unaltered during broadcast of one OFDM signal. So, here a low rank approximation is used with SSA. SSA can be viewed as SVD with overlapped data segment, which eliminates the above mentioned assumption.

B. Rank reduction of correlation matrix with the aid of SSA

As per the methodological steps of SSA, the matrix $R_{H_{CIR}H_{CIR}}$ is modified with its overlapping segments. Then SVD of channel correlation matrix is given by

$$R_{H_{CIR}H_{CIR}} = U\Lambda U^H \tag{15}$$

 $U = [u_0, u_1, \dots, u_{N-I}], u_0, u_1, \dots, u_{N-I}$ are column vectors. Λ contains all decomposed singular values in decreasing order as diagonal matrix $\Lambda = I[\lambda_0, \lambda_1, \dots, \lambda_{N-I}]$. As the first few represent the important components and last few related to unimportant one, so now the rank of matrix is reduced by considering first p singular values and remaining made to forcible zeros. Then equation (15) gets simplified to

$$\hat{H}_{CIR} = U \Gamma U^H \hat{H}_{CIRL} \tag{16}$$

where Γ contains modified diagonal matrix containing first few p values and remaining are zeros. This (16) represents the estimated channel.

C. SSA based denoising of received OFDM symbol using Pearson correlation and kurtosis

Singular spectrum analysis (SSA) decomposes the received OFDM symbol into different empirical orthogonal function (EOF) based on eigenvalue driven singular value decomposition (SVD). First few EOFs represent the important components of the signal and last EOFs represent the unimportant or noisy components of the signal. The selection of EOFs is based on either correlation or kurtosis values.

Under high SNR scenarios, EOFs with high correlation values represents the required signal and low correlation value indicates undesired noisy versions. In order to de-noise the OFDM signal, a correlation threshold is proposed here for selection of signal EOFs.

For effective de-noising, at typically low SNR situations, in addition to correlation coefficient we propose to use another statistical measure kurtosis is also used for selection of appropriate EOFs. In general, a high value of kurtosis indicates random component present in EOF. So, eliminating EOFs having high kurtosis values amounts reducing the random noise component present in the received OFDM symbol. For this purpose, a kurtosis threshold on is proposed for selection of useful number of EOFs.

The subsequent steps are proposed to de-noise the OFDM signal. The received signal is disintegrated into empirical orthogonal functions (EOF). EOFs will be generated by considering different eigenvalues during reconstruction process. By considering the best EOFs, the modified OFDM symbol will be constructed, which represents de-noised version. The best available EOF is selected based on the Pearson correlation (C_{xy}), a statistical measure.

$$C_{XY} = \frac{\text{cov}(X,Y)}{\sigma_X \sigma_Y} = \frac{\sum_{i=1}^{n} (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum_{i=1}^{n} (x_i - \overline{x})^2} \sqrt{\sum_{i=1}^{n} (y_i - \overline{y})^2}}$$
(17)

where \overline{x} , \overline{y} represent the mean of x and y respectively.

The correlation will be computed for all EOFs with recieved signal.

(i) Threshold for selection of reliable EOFs

The threshold for selection of signal EOFs is presented here using *mean* and stanadard deviation (*std*) of all evaluated correlation values.

$$\sigma_{th_{-c}} = mean(C_1, C_2, ..., C_i C_{N-1}) - std(C_1, C_2, ..., C_i C_{N-1})$$
(18)

where, C_i is the correlation value of i^{th} EOF with received signal; i=1, 2....N-1. So, as part of the de-noising process the EOFs above the computed threshold will be considered.

(ii) Kurtosis for selection of appropriate EOFs

For effective denoising, at typically low SNR situations, in addition to correlation coefficient we propose to use another statistical measure kurtosis(k) is also used for selection of appropriate EOFs.

$$k = \frac{E(x-\mu)^4}{\sigma^4} - 3 \tag{19}$$

where μ , σ are the mean and standard deviation of x. In general, the randomness of a typical signal can be measured by means Kurtosis.

(iii) Threshold on Kurtosis for selection of reliable EOFs

In general a high value of kurtosis indicates random component present in EOF. So, eliminating EOFs having high kurtosis values amounts reducing the random noise component present in the received OFDM symbol. For this purpose, a threshold $(\sigma_{th_{-}k})$ on kurtosis is proposed for selection of useful number of EOFs. This threshold $(\sigma_{th_{-}k})$ is taken as mean of kurtosis values plus the stanadard deviation of kurtosis values.

$$\sigma_{th_{-k}} = mean(k_1, k_2, \dots, k_i, \dots, k_{N-1}) + std(k_1, k_2, \dots, k_i, \dots, k_{N-1})$$
(20)

where k_i is kurtosis value of i^{th} EOF component; i=1, 2...N-1.

The de-noised signal ($y_d(n)$) is reconstructed using selected EOFs based on the σ_{th_c} , σ_{th_k} values. This $y_d(n)$ serves as input to the channel estimation algorithm proposed in this paper. The performance of the proposed channel estimation method is studied through different simulations presented in the following section.

IV. SIMULATION RESULTS AND ANALYSIS

The simulation results and its analysis were presented in this section. To evaluate the performance of the presented SSA based technique, the subsequent simulation parameters, are utilized. In simulations, different types of noisy scenarios were considered, such as impulsive noise and Gaussian noise. During de-noising, the received signal is decomposed in to their equivalent EOF components. Correlation co-efficient (C) and kurtosis (k) values for all EOFs are calculated and tabulated in Table II at SNR=23dB.

Correlation co-efficient between each decomposed EOF and received signal ku of each decomposed EOF. For the correlation values shown in Table II, mean is 0.49, standard deviation is 0.2144 and computed threshold as per (18) is σ_{th} $_c$ =0.2756.

TABLE I. SIMULATION PARAMETERS UTILIZED FOR PRESENTED SSA BASED TECHNIQUE VALIDATION [11]

Simulation Parameters	Considered values			
Carrier Frequency	5 GHz			
System bandwidth	80 MHz			
Sub carrier spacing	6.83 kHz			
Modulation	BPSK, QPSK, 16 QAM and 64 QAM			
N-point IFFT	256 - point IFFT			
Length of Cyclic Prefix	16 samples			
Doppler Frequency	100 Hz, 500 Hz and 1000Hz			

TABLE II. CALCULATED CORRELATION AND KURTOSIS VALUES OF DECOMPOSED EOFS @ SNR=23DB

	$E_1(n)$	$E_2(n)$	E ₃ (n)	E ₄ (n)	E ₅ (n)	E ₆ (n)	E ₇ (n)
C	0.721	0.7053	0.5621	0.5383	0.4945	0.2518	0.1562
\boldsymbol{k}	2.0271	3.5214	5.1617	4.7306	5.3852	7.1716	7.2764

Hence, the EOFs having correlation values above $\sigma_{th_c} = 0.2756$, i.e., the EOFs $E_I(n)$ to $E_S(n)$ are selected for de-noising. Similarly, in case of kurtosis values, mean is 5.0391, standrad deviation is 1.8779 and computed threshold as per (20) is $\sigma_{th_c} = 6.917$. Hence, the EOFs having kurtosis values below $\sigma_{th_c} = 6.917$, i.e., the EOFs $E_I(n)$ to $E_S(n)$ are selected for de-noising. It can be noticed here that both thresolds σ_{th_c} and σ_{th_c} selected same five EOFs $(E_I(n))$ to $E_S(n)$ for eleimination of uncorrelated and random noise components from the received OFDM symbol.

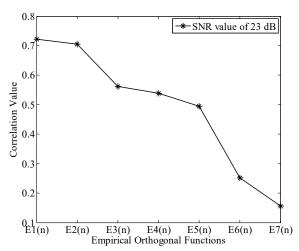


Fig. 4. Correlation values of different EOF with received OFDM symbol

At high SNRs, the correlation values, presented in Table-II, are monotonically decreasing in nature, as shown in Fig. 4. This makes the selection of EOFs very easy.

At low values of SNR say 3 dB, for same OFDMsymbol, the calculated correlation and kurtosis values are presented in Table-III. The correlation values, as shown in Fig. 5, are not monotonically decreasing. This makes the selection of EOFs difficult. Here the mean of correlation values is 0.4678,

standard deviation is 0.2671 and calculated threshold $\sigma_{th\ c} = 0.2007$.

TABLE III. CALCULATED CORRELATION AND KURTOSIS VALUES AT 3DB

	E ₁ (n)	E ₂ (n)	E ₃ (n)	E ₄ (n)	E ₅ (n)	E ₆ (n)	E ₇ (n)
PCC	0.1961	0.8192	0.6591	0.6294	0.5892	0.1944	0.1873
<i>k</i> u	2.1193	3.4742	5.1738	4.7576	5.4735	7.564	7.8764

As per the explained procedure the EOFs below threshold value should be removed. In that case, $E_1(n)$ to $E_3(n)$ are to be considered for final reconstruction of denoised OFDM signal discarding the first EOF. In fact, in SSA, the first component corresponds to first singular value and represents the important component of the signal. Hence reconstruction without $E_1(n)$ will not give approprite denoised signal. In such situations at low SNRs, the kurtosis will become a useful measure.

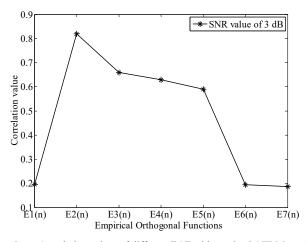


Fig. 5. Correlation values of different EOF with received OFDM symbol for SNR of 3 dB

The mean of kurtosis values is 5.2055, standard deviation is 2.0612 and computed threshold $\sigma_{th_{-k}}$ =7.2668. Hence, the EOFs having kurtosis values below $\sigma_{th_{-k}}$ =7.2668 will be considered. This selection will include the first EOF. Finally, the denoised signal is reconstructed using $E_1(n)$ to $E_5(n)$. So kurtosis is a useful mesure for selection of EOFs at low values of SNR.

To establish this concept, further simulations are carried out at different SNRs . The result presented in Fig. 6, reveals that correlation is capable of identifying useful EOFs only for SNR $\geq 12 dB, \ \,$ whereas for SNRs $< 12 dB, \ \,$ kurtosis will be useful measure to identify useful EOFs.

The resulting denoised signal $y_d(n)$ will used for further precessing for channel estimation by proposed method. One of the prime merits of the proposed SSA based technique is that use of overlapping data segments.

The constellation methods such as BPSK, QPSK, 16-QAM and 64-QAM are considered for BER computation. The propsed SSA based technique performance is compared with LSE [3], MMSE [7], SVD [1] methods. The simulations are presented in Fig. 7 to Fig. 8 to show the superiority of the proposed method. It can be seen from Fig. 7, under BPSK

constellation that there is a linear trend among methods for all SNR vaues. For a BER of 10⁻³, the proposed SSA based signal processing method provides an improvement of 7 dB compared to LS, 4 dB compared to MMSE and 1.5 dB for BPSK constellation.

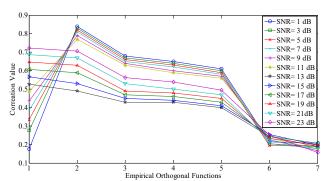


Fig. 6. Correlation values of EOFs with received OFDM symbol for different values SNR

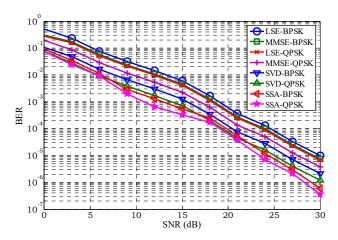


Fig. 7. BER plot of OFDM transceiver using BPSK and QPSK modulation Schemes

In Fig. 7, for QPSK constellation, for small SNR values there is a extra enhancement than higher SNR values. Here for a BER of 10⁻³, the proposed method outperforms the LSE method by 8 dB, MMSE by 6 dB and SVD by 3 dB. For 16-QAM, the proposed method has shown an improved performance by 6 dB over LSE, 5 dB over MMSE and 3 dB over SVD based methods as depicted in Fig. 8.

From Fig. 8 for 64 QAM constellation, it can be seen an enhancement of 7 dB, 4 dB and 2 dB respectively as compared to LSE, MMSE and SVD based methods. All the simulations aimed at studying the efficacy of the proposed method have clearly demonstrated that comparing to LSE, MMSE and SVD based methods,the propsed SSA based method provides better performance.

In addition, the mean square error (MSE) of CIR estimation is also evaluated and shown in Fig. 9, indicates an improvement for SSA based technique.

With the addition of de-noising stage the performance of presented SSA based technique is further improved. The results presented in Fig. 10 establish the fact that it effectively reduces the signal noise, and hence improves the estimation performance. With this denoising approach, the MSE of

channel estimator has been further improved which translated to approximately 1 dB improvement in SNR at the receiver.

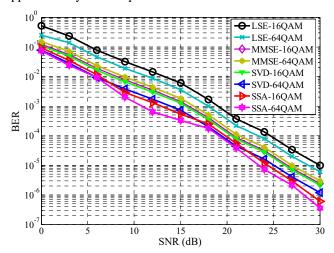


Fig. 8. Comparison of BER: 16 QAM and 64-QAM constellation

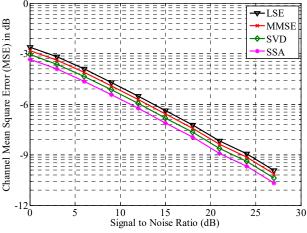


Fig. 9. Channel MSE comparison

In addition to outperforming the existing methods, this additional 1 dB SNR improvement is achieved at the cost of computations involved during the de-noising process.

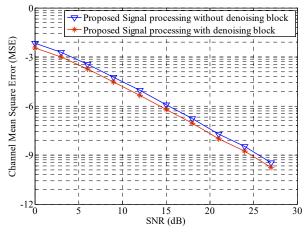


Fig. 10. Channel MSE evaluation with and without inclusion of de-noising block

The normalized root mean square error (NRMSE) of channel impulse response is computed for different channel environments, to further launch the effectiveness of the presented SSA based technique.

NRMSE (dB) = 20
$$log_{10} \left[\sqrt{\frac{\sum_{n=0}^{N} \left[h_{CIR}(n) - \hat{h}_{CIR}(n) \right]^{2}}{\sum_{n=0}^{N} \left[h_{CIR}(n) \right]^{2}}} \right]$$
 (21)

where N is length of the CIR, $h_{CIR}(n)$ and $\hat{h}_{CIR}(n)$ is assumed and estimated impulse response respectively.

TABLE IV. NRMSE (DB) COMPUTED UNDER DIFFERENT CHANNEL ENVIRONMENTS

	I	II	III	IV	V
NRMSE (dB)	-8.29	-5.63	-6.23	-8.41	-6.25

The evaluated NRMSE values, as shown in Table IV, are very low and indicate the effectiveness of the proposed SSA based technique for OFDM CE.

V. CONCLUSION

A method based on singular spectrum analysis (SSA) has been presented here for OFDM channel estimation (CE). With the use of overlapping data segments in the processing steps of SSA makes it useful for OFDM CE under fast fading conditions. In the proposed algorithm, the initial CE is computed with the aid of traditional LMMSE algorithm, and then further channel is evaluated by considering the low rank eigenvalue approximation of channel matrix using SSA. The BER and channel error MSE results were compared with wellestablished CE methods such as LSE, MMSE and SVD. Simulation results revealed that the method attained 7 dB improvement compared to common LSE, 5 dB over MMSE and almost 3 dB improvement over SVD. SSA used here for two purposes i.e. CE and de-noising, which further improved estimation accuracy. As part of de-noising purpose, SSA decomposed the received OFDM symbol into different empirical orthogonal functions (EOFs) as in the order of singular values and noisy reduced signal was combined with either highly correlated EOFs or kurtosis computed EOFs. Correlated EOFs were identified based on either with threshold on correlation or with threshold on kurtosis calculated between received signal and EOFs. It was demonstrated that the correlation coefficients worked well in identifying useful EOFs only up to moderate SNR ≥ 12dB. For low SNR<12 dB, kurtosis was found to be a useful measure for identifying the useful EOFs. With this de-noising approach, the MSE of channel estimator has been further improved which translated to approximately 1 improvement in signal-to-noise ratio at the receiver. In addition to outperforming the existing methods, this additional 1 dB SNR improvement was achieved at the cost of computations involved during the de-noising process. Complete simulation analysis under all fading channels

revealed the efficacy of the proposed system. The real time computational complexity analysis will fully explore effectiveness of the proposed method will be the possible future scope.

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